Clustering refers to a broad set of techniques for finding subgroups in a data set.
For instance, suppose we have a set of n observations, each with p features. The n observations could correspond to tissue samples for patients with breast cancer and the p features could correspond to
We may have reason to believe there is heterogeneity among the n observations.
This is unsupervised because

	Both	clustering an	nd PCA	seek to	simplify	the dat	a via a	a small	number	of su	ımmaries.
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- PCA
- Clustering

Since clustering is popular in many fields, there are many ways to cluster.

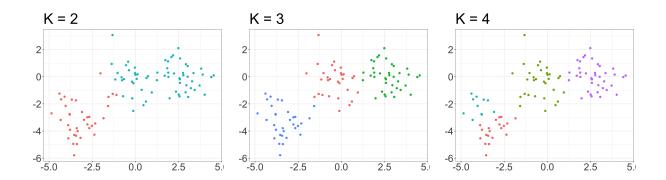
• *K*-means clustering

• Hierarchical clustering

In general, we can cluster observations on the basis of features or we can cluster features on the basis of observations.

3.1 K-Means Clustering

Simple and elegant approach to parition a data set into K distinct, non-overlapping clusters.

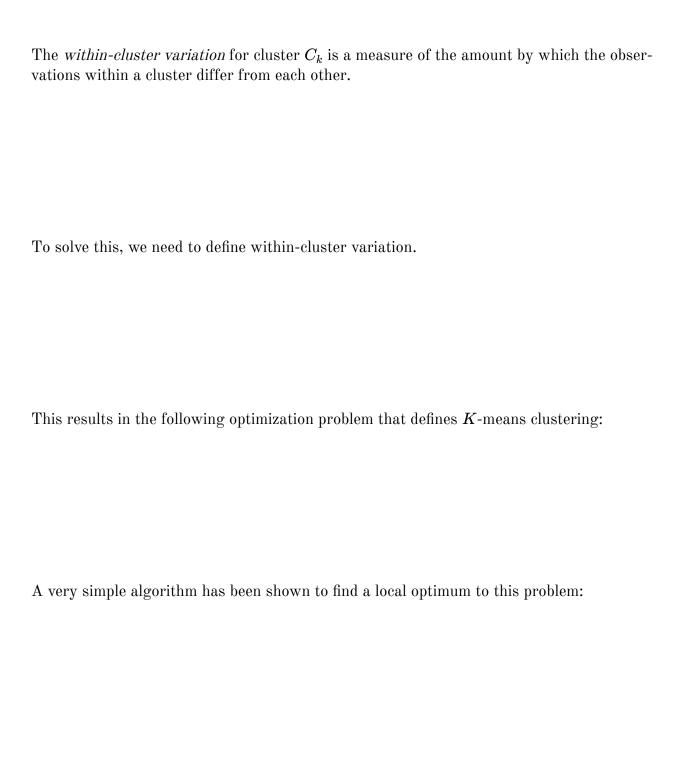


The K-means clustering procedure results from a simple and intuitive mathematical problem. Let C_1, \ldots, C_K denote sets containing the indices of observations in each cluster. These satisfy two properties:

1.

2.

Idea:

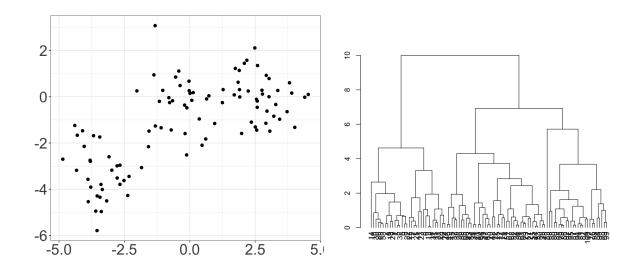


3.2 Hierarchical Clustering

One potential disadvantage of K-means clustering is that it requires us to specify the number of clusters K. Hierarchical clustering is an alternative that does not require we commit to a particular K.

We will discuss bottom-up or agglomerative clustering.

3.2.1 Dendrograms

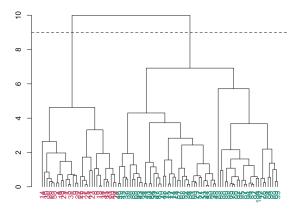


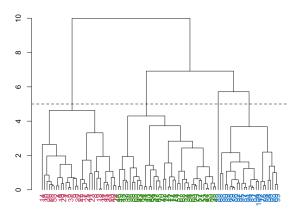
Each leaf of the dendrogram represents one of the 100 simulated data points.

As we move up the tree, leaves begin to fuse into branches, which correspond to observations that are similar to each other.

For any two observations, we can look for the point in the tree where branches containing those two observations are first fused.

How do we get clusters from the dendrogram?



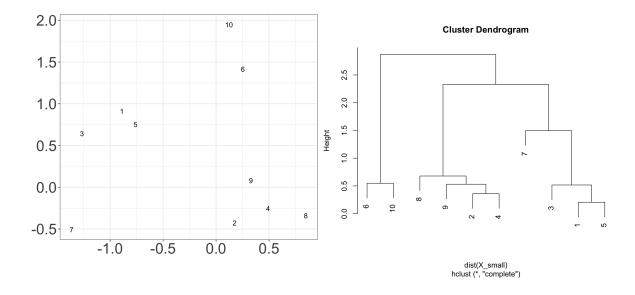


The term *hierarchical* refers to the fact that clusters obtained by cutting the dendrogram at a given height are necessarily nested within the clusters obtained by cutting the dendrogram at a greater height.

3.2.2 Algorithm

First, we need to define some sort of dissimilarity metric between pairs of observations.

Then the algorithm proceeds iteratively.



4.

More formally, One issue has not yet been addressed. How do we determine the dissimilarity between two clusters if one or bother of them contains multiple observations? 1. 2. 3.

3.2.3 Choice of Dissimilarity Metric

3.3 Practical Considerations in Clustering

In order to perform clustering, some decisions should be made.

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Each of these decisions can have a strong impact on the results obtained. What to do?