

Chapter 8: Tree-Based Methods

We will introduce tree-based methods for regression and classification.

These involve segmenting the predictor space into a number of simple regions To make a prediction for an observation, we will now the mean or made of the fraining observations in the regions the which it belongs.

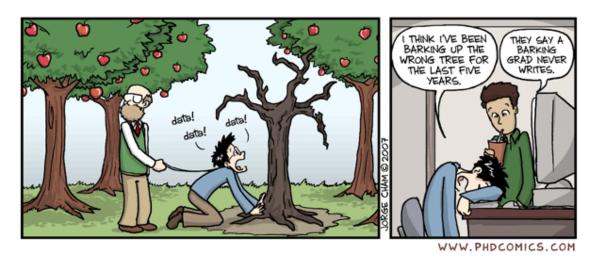
The set of splitting rules can be summarized in a tree \Rightarrow "decision trees".

- simple and useful for interpretation

- not competetive w/ other supervised approaches (eg. lasso) for prediction.

> bagging, random forests,

Combining a large number of trees can often result in dramatic improvements in prediction accuracy at the expense of interpretation.



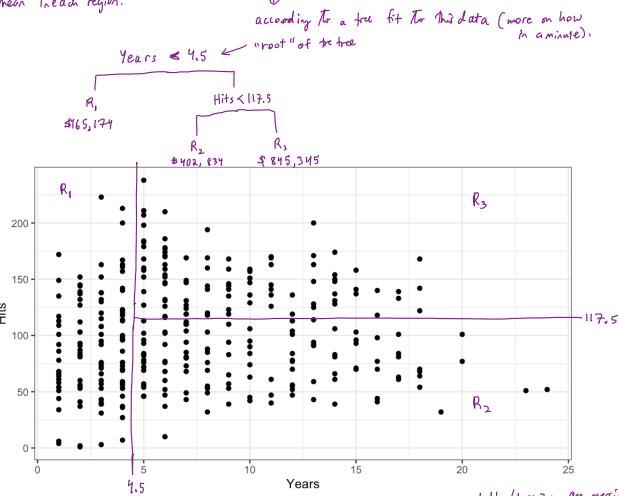
Credit: http://phdcomics.com/comics.php?f=852

Decision trees can be applied to both regression and classification problems. We will start with regression.

1 Regression Trees

Example: We want to predict baseball salaries using the Hitters data set based on Years (the number of years that a player has been in the major leagues) and Hits (the number of hits he made the previous year).

We could make a series of splithing rules to create regions and predict scharge as the mean ineach region.



The predicted salary for players is given by the mean response value for the players in that nice graphical box. Overall, the tree segments the players into 3 regions of predictor space.

terminology: Riskz, R3 = terminal nodes or leave of the tree

points along he tree where space is split = internal nodes

segments of tree that connect hodes = bronches.

interpretation: Years is the most important factor in determining salary

La given that a player is experienced, # hits in previou yearplays a cole in his salary: Thits, Tsalay.

La given that a player is not experienced, # hits choose not affect your salary.

quantitative of

We now discuss the process of building a regression tree. There are to steps:

out of possible values for X17. ... Xp

1. Divide predictor space

into J distinct and non-owlapping regions River, Ro

2. Predict

For every observation that falls into region his he make The same prediction, the mean of the response Y for training values in Ri

How do we construct the regions R_1, \ldots, R_J ? How to divide the predictor space? regions could have any Shape: but that is two hard (to do + interpret)

=> divide predictor space Noto high dimensional rectangles or boxes

The goal is to find boxes R_1, \ldots, R_J that minimize the RSS. $= \sum_{j=1}^{J} \sum_{i \in R_j} (\gamma_i - \hat{\gamma}_{R_j})^2$ where $\hat{\gamma}_{R_j} = \frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{i \in R_j} (\gamma_i - \hat{\gamma}_{R_j})^2$ where $\hat{\gamma}_{R_j} = \frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{i \in R_j} (\gamma_i - \hat{\gamma}_{R_j})^2$ where $\hat{\gamma}_{R_j} = \frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{i \in R_j} (\gamma_i - \hat{\gamma}_{R_j})^2$ where $\hat{\gamma}_{R_j} = \frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{i \in R_j} (\gamma_i - \hat{\gamma}_{R_j})^2$ where $\hat{\gamma}_{R_j} = \frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{i \in R_j} (\gamma_i - \hat{\gamma}_{R_j})^2$ where $\hat{\gamma}_{R_j} = \frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{i \in R_j} (\gamma_i - \hat{\gamma}_{R_j})^2$ where $\hat{\gamma}_{R_j} = \frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{i \in R_j} (\gamma_i - \hat{\gamma}_{R_j})^2$ where $\hat{\gamma}_{R_j} = \frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{i \in R_j} (\gamma_i - \hat{\gamma}_{R_j})^2$ where $\hat{\gamma}_{R_j} = \frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{j=1}^{N} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{j=1}^{N} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{j=1}^{N} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{j=1}^{N} \sum_{j=1}^{N} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{j=1}^{N} \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{j=$ every possible partition.

=> take top-down, greedy approach called recursive binary splithing

The approach is *top-down* because

We start at the top of the tree (where all observations belong to a single region) and successively split the predictor space.

La each split is indicated bia two new branches in the tree.

The approach is *greedy* because

at each step of he building process, he list split is made at not partial a step. Ly not looking ahead to make a split plat vill lead to a settle tree layer.

In order to perform recursive binary splitting,

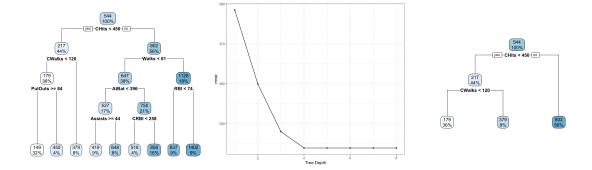
Ly We consider all possible X1,-, Xp and all possible cutpoints then choose predictor & cutpoint so tree has lowest RSS.

The process described above may produce good predictions on the training set, but is likely to overfit the data.

A smaller tree, with less splits might lead to lower variance and better interpretation at the cost of a little bias.

A strategy is to grow a very large tree T_0 and then prune it back to obtain a subtree.

Algorithm for building a regression tree:



2 Classification Trees

A classification tree is very similar to a regression tree, except that it is used to predict a categorical response.
For a classification tree, we predict that each observation belongs to the <i>most commonly</i> occurring class of training observation in the region to which it belongs.
The task of growing a classification tree is quite similar to the task of growing a regression tree.
It turns out that classification error is not sensitive enough.
When building a classification tree, either the Gini index or the entropy are typically used to evaluate the quality of a particular split.

3 Trees vs. Linear Models

Regression and classification trees have a very different feel from the more classical approaches for regression and classification.

Which method is better?

3.1 Advantages and Disadvantages of Trees

4 Bagging

1 Dagging
Decision trees suffer from high variance.
Bootstrap aggregation or bagging is a general-purpose procedure for reducing the variance of a statistical learning method, particularly useful for trees.
So a natural way to reduce the variance is to take many training sets from the population, build a separate prediction model using each training set, and average the resulting predictions.
Of course, this is not practical because we generally do not have access to multiple training sets.

While bagging can improve predictions for many regression methods, it's particularly useful for decision trees.

These trees are grown deep and not pruned.

How can bagging be extended to a classification problem?

4.1 Out-of-Bag Error

There is a very straightforward way to estimate the test error of a bagged model, without the need to perform cross-validation.

10 4 Bagging

4.2 Interpretation

5 Random Forests

size m.

$Random\ forests$ provide an improvement over bagged trees by a small tweak that decorrelates the trees.
As with bagged trees, we build a number of decision trees on bootstrapped training samples.
In other words, in building a random forest, at each split in the tree, the algorithm is not allowed to consider a majority of the predictors.
The main difference between bagging and random forests is the choice of predictor subse

6 Boosting

Boosting is another approach for improving the prediction results from a decision tree.

While bagging involves creating multiple copies of the original training data set using the bootstrap and fitting a separate decision tree on each copy,

Boosting does not involve bootstrap sampling, instead each tree is fit on a modified version of the original data set.

Boosting has three tuning parameters:

1.

2.

3.