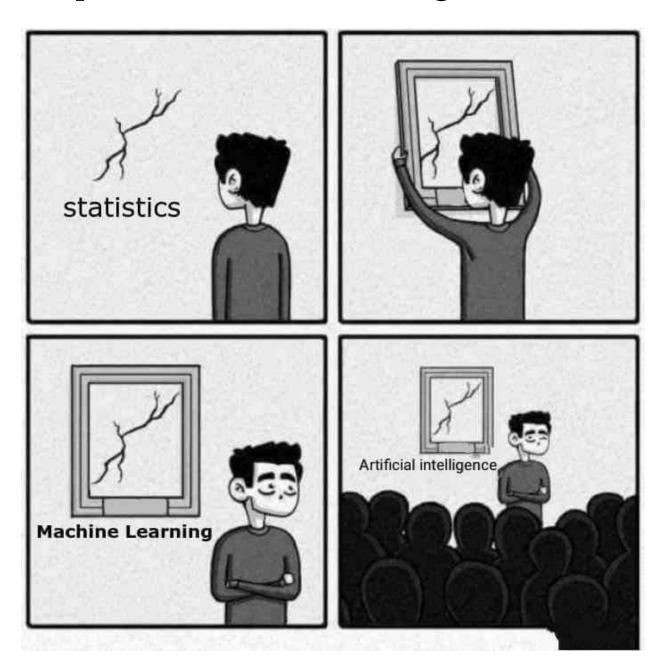
Chapter 2: Statistical Learning



Credit: https://www.instagram.com/sandserifcomics/

Statistical machine learning is more than "just" statistics and more than "just" machine learning.

We choose methods based on data AND our goals.

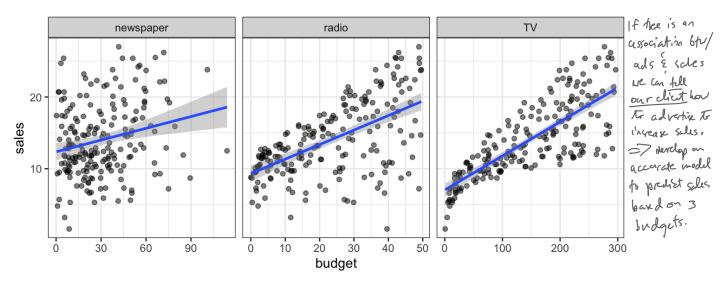
1 What is Statistical Learning?

A scenario: We are consultants hired by a client to provide advice on how to improve sales

of a product.

| ×, | Xz | Xz | γ |
|-------|-------|-----------|-------|
| TV | radio | newspaper | sales |
| 230.1 | 37.8 | 69.2 | 22.1 |
| 44.5 | 39.3 | 45.1 | 10.4 |
| 17.2 | 45.9 | 69.3 | 9.3 |
| 151.5 | 41.3 | 58.5 | 18.5 |

We have the advertising budgets for that product in 200 markets and the sales in those markets. It is not possible to increase sales directly, but the client can change how they budget for advertising. How should we advise our client?



More generally - observe quantitative variable Y and p predictors X12-1, Xp

Assume prese is some relationship between predictors and response,

$$Y = f(X) + e.$$

$$C = f(X) + e$$

f con shrolve more than I imput variable (eg. TV, radio, newsupaper).

Essentially, $statistical\ learning$ is a set of approaches for estimating f.

1.1 Why estimate f?

There are two main reasons we may wish to estimate f. our goals for an analysis.

Prediction

In many cases, inputs X are readily available, but the output Y cannot be readily obtained (or is expensive to obtain). In this case, we can predict Y using

prediction for
$$\Rightarrow \hat{Y} = \hat{f}(X)$$
 (respect error averages to 0)

In this case, \hat{f} is often treated as a "black box", i.e. we don't care much about it as long as it yields accurate predictions for Y.

The accuracy of \hat{Y} in predicting Y depends on two quantities, reducible and irreducibleerror.

reducible: f is not a perfect estimate of f, but we can reduce error by an using an appropriate state learning method to estimate f.

isceducible: Even if f was estimated perfectly we would still have some error because Y is a fundion of e! We cannot reduce this no matter how well he estimate f.

Why? e cordains vameasured variables that would be unful for predicting Y. Cossider an estimate f and predictors X (fixed).

$$E[(y-\hat{y})^2] = E[(f(x)+e-\hat{f}(x))^2]$$

$$= [f(x)-\hat{f}(x)]^2 + Var(e)$$
reducible.

expected value of

We will focus on techniques to estimate f with the aim of <u>reducing the reducible error</u>. It is important to remember that the irreducible error will always be there and gives an upper bound on our accuracy. (always unknown in practice).

Inference

Sometimes we are interested in understanding the way Y is affected as X_1, \ldots, X_p change. We want to estimate f, but our goal isn't to necessarily predict Y. Instead we want to understand the relationship between X and Y.

- 1. Which predictors are associated of response?
- 2. What is relationship by response and each predictor?
- 3. Can relationship be adequately summarized by a linear equation or is it more complicated?

To return to our advertising data,

Inference: - which wedia contribute to sales?
- which media generate the biggest boost in sales?
- how much increase in sales is associated of a given increase in TV advertisity?

prediction: - What can I expect sales to be if sped \$200k on TV and 40 on newspaper & radio?

Depending on our goals, different statistical learning methods may be more attractive.

e.g. Linear moduls allow for interpretable inference but maybe not the most accurate prediction.

non-linear approaches car provide accurate predictions but much less inferentable.

1.2 How do we estimate f? I want to estimate f who have obsered a different data points and want to estimate f which some state of the following data" train to be have observed a different data points and want to estimate f which some state of the following data" train to be have observed a different data points and want to estimate f which some state of the following data" train to be have observed a different data points and want to estimate f which some state of the following data" to be have observed an different data points and want to estimate f which is the first data and the following data.

apply a statistical learning method to fraining data To extinute unknown f.

In other words, find a function \hat{f} such that $Y \approx \hat{f}(X)$ for any observation (X,Y). We can characterize this task as either *parametric* or *non-parametric*

Parametric

- 1. Make an assumption about shape of f, paramoters e.g. $f(x) = \beta$, $+\beta x_1 + ... \beta x_p$.
- 2. Use training data to fif or "train" he model.

 e.g. estimate fo, \$1, -, \$p with ordinary least squares (one of many options).

This approach reduced the problem of estimating f down to estimating a set of parameters.

Why?

This simplifies the problem of estimating f.

Disadratage:

What if shape we doose in not similar to f? Then the estimate (and padiations) will be poor.

We can fing more flexible model, this means more para notes can lead the overfithing: fithing excess in training data too closely.

shepe.

Non-parametric

Non-parametric methods do not make explicit assumptions about the functional form of f. Instead we seek an estimate of f that is as close to the data as possible without being too wiggly.

Why?

Advantage

= fit wide range of possible shapes

- no restrictions on shape => con't
assure wrong shape.

Disadventages

- haven't simplified the postern!

>> need a lot of data.

e.g. splines (ch. 7)

1.3 Prediction Accuracy and Interpretability

Of the many methods we talk about in this class, some are less flexible – they produce a small range of shapes to estimate f.

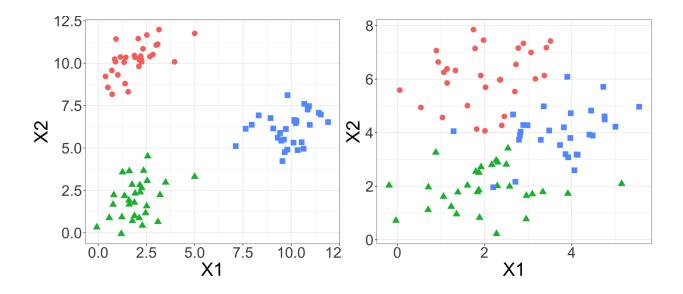
Why would we choose a less flexible model over a more flexible one?

2 Supervised vs. Unsupervised Learning

 ${\it Most statistical learning problems are either {\it supervised} or {\it unsupervised} - }$

What's possible when we don't have a response variable?

- We can seek to understand the relatopnships between the variables, or
- We can seek to understand the relationships between the observations.



Sometimes it is not so clear whether we are in a supervised or unsupervised problem. For example, we may have m < n observations with a response measurement and n - m observations with no response. Why?

In this case, we want a method that can incorporate all the information we have.

3 Regression vs. Classification

Variables can be either quantitative or categorical.

Examples -Age Height Income Price of stock Brand of product purchased Cancer diagnosis Color of cat We tend to select statistical learning methods for supervised problems based on whether the response is quantitative or categorical. However, when the predictors are quantitative or categorical is less important for this choice.