

Chapter 8: Tree-Based Methods

We will introduce *tree-based* methods for regression and classification.

- These involve segmenting the predictor space into a number of simple regions.
- to make a prediction for an observation, we use mean or mode of training data in the region to chick it belongs.

The set of splitting rules can be summarized in a tree \Rightarrow "decision trees".

- simple and useful for interpretation = not competitive w/ one supervise approaches (e.g. lasso) for prediction. >> bagging, readom for ests, boosting. (loter)

Combining a large number of trees can often result in dramatic improvements in prediction accuracy at the expense of interpretation.



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Decision trees can be applied to both regression and classification problems. We will start with regression.

1 Regression Trees

stort with Example: We want to predict baseball salaries using the Hittgers data set based onYears (the number of years that a player has been in the major leagues) and Hits (the "root" of the tree number of hits he made the previous year). Years < 4,5 We can make a series of splithing rules to create regions and predict salenzy as the mean in each region. Hits 5117.5 R_3 A, A, \$ 845, 345 \$165,174 \$402,834 R3 R. 200 150 Hits 117.5 R2 100 -50 0 0 5 10 . 15 20 25 4.5 Years

The predicted salary for players is given by the mean response value for the players in that box. Overall, the tree segments the players into 3 regions of predictor space.

ry"

We now discuss the process of building a regression tree. There are to steps:

1. Divide the predictor space

2. Predict For every observation that falls into region R: we make the same prediction, the mean of response Y for training values in hj.

How do we construct the regions R_1, \ldots, R_J ? How the divide the predictor spece?

The goal is to find boxes R_1, \ldots, R_J that <u>minimize</u> the RSS. $= \sum_{j=1}^{J} \sum_{i \in R_j} (y_i - \hat{y}_{R_j})^2$ Unfortunately it is computationally infeasible to shre. (blc biside every possible pertition)

The approach is *top-down* because

The approach is *greedy* because



The process described above may produce good predictions on the training set, but is likely to overfit the data.

because resulting tree may be too complex

A smaller tree, with less splits might lead to lower variance and better interpretation at the cost of a little bias.

Better idea:

A strategy is to grow a very large tree T_0 and then *prune* it back to obtain a *subtree*. grad: substrue hat lends the lowest test error rate. Could use CV the estimate error for solution: "cost randomt. " solution: "cost composity pruning" at a "weakest link pruning" possible induces). Consider a sequence of trees indexed by a non-negative twiz parameter d. For each relate of X, 3 a corresponding subtree TCTo sit. $\sum_{m=1}^{|T|} \sum (y_i - \hat{y}_{R_m})^2 + \alpha |T| \text{ is as small as possible.}$ $m = (x_i \in R_m) \quad \text{for mind nodes of the there.}$ Am = mith terminal hode tegion when Q=0 ýpm = predicted response for Rm d undrol hade off between subject's complexity of tit to training date of => price + pay for d undrol hade off between subject's complexity of tit to training date dt => price + pay for having many terminal hodes => smiller tree Select & via CV, then use full data set & chosen a to get subtree.

Algorithm for building a regression tree:

(1) Use recursive binary splitting to grow a large tree or training data, stopping only cleaced torained wode has force than some aninimum # 4 dosorctions.
(2) Apply cost complexity opening the large tree to sub a sequence of less trees, as a Surchim of d.
(3) Use to fold CV to choose d

Divide training data into k filds, for each to the sub a sequence of less trees, as a Surchim of d.
(b) evaluate into k filds, for each to the sub a sequence of less trees, as a Surchim of d.
(b) evaluate into k filds, for each to the subscription of d.
(b) evaluate into k filds, for each to the subscription of d.
(c) report (1) to (2) on all but the fild.
(b) evaluate into the subscription of d and pick data university for each value of d and pick data university.

(c) evaluate the form (2) that unresponds to (2) from (3).



2 Classification Trees

A *classification tree* is very similar to a regression tree, except that it is used to predict a categorical response.

For a classification tree, we predict that each observation belongs to the *most commonly occurring class* of training observation in the region to which it belongs.

The task of growing a classification tree is quite similar to the task of growing a regression tree.

It turns out that classification error is not sensitive enough.

When building a classification tree, either the Gini index or the entropy are typically used to evaluate the quality of a particular split.

3 Trees vs. Linear Models

Regression and classification trees have a very different feel from the more classical approaches for regression and classification.

Which method is better?

3.1 Advantages and Disadvantages of Trees

4 Bagging

Decision trees suffer from high variance.

Bootstrap aggregation or *bagging* is a general-purpose procedure for reducing the variance of a statistical learning method, particularly useful for trees.

So a natural way to reduce the variance is to take many training sets from the population, build a separate prediction model using each training set, and average the resulting predictions.

Of course, this is not practical because we generally do not have access to multiple training sets.

While bagging can improve predictions for many regression methods, it's particularly useful for decision trees.

These trees are grown deep and not pruned.

How can bagging be extended to a classification problem?

4.1 Out-of-Bag Error

There is a very straightforward way to estimate the test error of a bagged model, without the need to perform cross-validation.

4.2 Interpretation

5 Random Forests

Random forests provide an improvement over bagged trees by a small tweak that decorrelates the trees.

As with bagged trees, we build a number of decision trees on bootstrapped training samples.

In other words, in building a random forest, at each split in the tree, the algorithm is not allowed to consider a majority of the predictors.

The main difference between bagging and random forests is the choice of predictor subset size m.

6 Boosting

Boosting is another approach for improving the prediction results from a decision tree.

While bagging involves creating multiple copies of the original training data set using the bootstrap and fitting a separate decision tree on each copy,

Boosting does not involve bootstrap sampling, instead each tree is fit on a modified version of the original data set.

Boosting has three tuning parameters:

1.

2.

3.